

American University of Beirut
Department of Electrical and Computer Engineering

EECE 320 – Digital Systems Design
 Assignment 2

16/10/2007

Suggested problems: Solve the drill problems 4.6-4.11 of chapter 4.

Problem 1: Simplify the Boolean expressions to a minimum number of literals:

- a) $wxy' + wy'z' + wx'z'$
- b) $ABC + A'B + ABC'$
- c) $(BC' + A'D)(AB' + CD')$
- d) $A'B(D' + C'D) + B(A + A'CD)$ (reduce to one literal)
- e) $(A' + C)(A' + C')(A + B + C'D)$ (reduce to 4 literals)

Problem 2: Find the complement of the following functions

- a) $AB(C'D + CD') + A'B'(C' + D)(C + D')$
- b) $(x + y' + z)(x' + z')(x + y)$

Problem 3: Draw the following functions using OR gates and inverters only.

- a) $F = x'y' + x'z + y'z$
- b) $G = (y + z')(x + y)(y' + z)$

Problem 4: Repeat problem 3 using AND gates and inverters only.

Problem 5: For the Boolean function F given in truth table, find the following:

w	x	y	z	F
0	0	0	0	0
0	0	0	1	1
0	0	1	0	0
0	0	1	1	0
0	1	0	0	0
0	1	0	1	1
0	1	1	0	1
0	1	1	1	1
1	0	0	0	0
1	0	0	1	1
1	0	1	0	1
1	0	1	1	1
1	1	0	0	0
1	1	0	1	1
1	1	1	0	1
1	1	1	1	1

- a) F as a Minterm list using Σ notation
- b) F as a Canonical sum
- c) F as a Maxterm list using Π notation
- d) F as a Canonical product
- e) The complement of F as sum of minterms
- f) Simplify F to a minimum number of literals

Problem 6: Convert the following expressions into 1) minimal sum of products 2) minimal product of sums and 3) sum of minterms. (Draw the corresponding truth table)

a) $(AB+C)(B+C'D)$

b) $x'+x(x+y')(y+z')$

Assignment 2

Solution

1) a) $wxy' + wy'z' + wx'z' = w(xy' + x'z' + y'z') = w(xy' + x'z')$
By consensus

b) $ABC + A'B + ABC' = AB(C + C') + A'B = AB + A'B = B$

c) $(BC' + A'D)(AB' + CD') = AB'B'C' + AB'A'D + CD'BC' + CD'A'D$
 $= 0$

d) $A'B(D' + C'D) + B(A + A'CD) = B(A'D' + A'C'D + A + A'CD)$
 $= B(A'D' + A + A'D(C' + C)) = B(A + A'(D' + D)) = B(A + A') = B$

e) $(A' + C)(A' + C')(A + B + C'D) = (A' + CC')(A + B + C'D)$
 $= A'(A + B + C'D) = A'B + A'C'D = A'(B + C'D)$

2) a) $[AB(C'D + CD') + A'B'(C' + D)(C + D')]'$

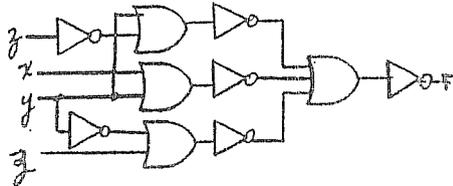
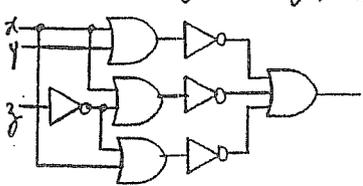
$[(A' + B') + (C + D')(C' + D)][(A + B) + C'D' + C'D]$

b) $(x + y' + z)(x' + z')(x + y) = x'y'z' + xz + x'y'$

3)

(a) $F = x'y' + x'z + y'z$
 $= (x+y)' + (x+z)' + (y+z)'$

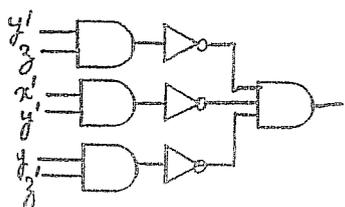
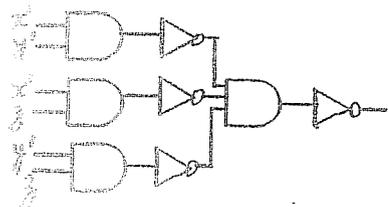
(b) $F = (y+z')(x+y)(y'+z)$
 $= [(y+z)' + (x+y)' + (y'+z)']'$



4)

(a) $F = x'y' + x'z + y'z$
 $= [(x'y')' + (x'z)' + (y'z)']'$

(b) $F = (y+z')(x+y)(y'+z)$
 $= (y'z)' + (x'y)' + (y'z)'$



Problem 5

$$a) F = \sum_{w,x,y,z} (1, 5, 6, 7, 9, 10, 11, 13, 14, 15)$$

$$b) F = w'x'y'z + w'x'y'z' + w'x'yz + w'x'yz' + wx'y'z + wx'y'z' + wx'yz + wx'yz' + wx'yz' + wx'yz' + wx'yz'$$

$$c) F = \prod_{w,x,y,z} (0, 2, 3, 4, 8, 12)$$

$$d) F = (w+x+y+z)(w+x+y'+z)(w+x+y'+z')(w+x'+y+z)(w'+x+y+z)(w'+x'+y+z)$$

$$e) F' = \sum_{w,x,y,z} (0, 2, 3, 4, 8, 12) \quad (\text{Since minterms of } F' \text{ are the maxterms of } F)$$

$$f) y'z \left(\underbrace{w'x' + w'x + wx' + wx}_{1} \right) + yz' \left(\underbrace{w'x + wx + wx'}_{x+w} \right) + yz \left(\underbrace{w'x + wx + wx'}_{x+w} \right) =$$

$$F = y'z + yz'(x+w) + yz(x+w)$$

$$F = y'z + y(x+w) \quad \dots \quad 5 \text{ literals.}$$

Problem 6

$$\begin{aligned} a) (A+B)(B+C'D) &= AB + ABC'D + BC + 0 \\ &= AB + BC \quad (\text{Sum of Products}) \\ &= B(A+C) \quad (\text{Product of Sums}) \end{aligned}$$

truth table

A	B	C	D	F
0	0	0	0	0
0	0	0	1	0
0	0	1	0	0
0	0	1	1	0
0	1	0	0	0
0	1	0	1	0
0	1	1	0	1
0	1	1	1	1
1	0	0	0	0
1	0	0	1	0
1	0	1	0	0
1	0	1	1	0
1	1	0	0	1
1	1	0	1	1
1	1	1	0	1
1	1	1	1	1

$$F = \sum_{A,B,C,D} (6, 7, 12, 13, 14, 15)$$

$$b) F = x' + x(x+y')(y+z') = \underbrace{(x'+x)}_1 (x' + (x+y')(y+z'))$$

$$F = x' + xy + y'z'$$

$$\text{since } x' + xy = x' + y \quad \left(\underbrace{(x'+x)}_1 (x'+y) = x'+y \right)$$

~~and~~ Then

$$F = x' + \underbrace{y + y'z'} = x' + y + z' \quad \leftarrow \begin{array}{l} \text{SOP and} \\ \text{POS} \end{array}$$

$$F = \sum_{x,y,z} (0, 1, 2, 3, 4, 6, 7)$$

(since $F = \text{Maxterm } 5$)